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Abstract

In this paper, we build a fully specified parsimonious Sraffian supermultiplier stockflow consistent model (SSM-SFC) with two non-capacity creating autonomous expenditures: residential investment and debt-financed consumption. Our model represents a closed economy without government with workers and capitalists households and only the latter are not credit constrained. The introduction of residential investment implies that our SSM-SFC model has two real assets: firms' productive capital and households' real estate. In our model, residential investment growth rate responds to changes of house price inflation. The numerical simulation experiments shows that our model keeps the main standard Sraffian supermultiplier growth models results. As a particular result, an increase of residential investment growth rate implies a decrease of real estate share in total real assets. Inspired by the recent U.S. bubble episode, we plug house price inflation data (1992-2019) into our model. Although simple, our numerical simulations are capable to reproduce some stylized facts such as residential investment leading the business cycle and capital accumulation and a clockwise pattern between non-capacity creating autonomous expenditures and capacity utilization rate.

Keywords: Residential Investment; Sraffian supermultiplier; Asset bubble; Stock-Flow Consistent approach; US Economy **JEL:** B51, E11, E12, E17, G51, O41, O51

Resumo

Neste artigo, desenvolvemos um modelo supermultiplicador sraffiano parcimonioso com consistência entre fluxos e estoques (SSM-SFC) com dois gastos autônomos não criadores de capacidade produtiva: investimento residencial e consumo financiado por crédito. Nosso modelo representa uma economia fechada e sem governo com famílias de trabalhadores e de capitalistas no qual somente estas últimas não possuem restrição de crédito. A inclusão do investimento residencial implica um modelo SSM-SFC com dois ativos reais: capital das firmas e imóveis das famílias. Em nosso modelo, a taxa de crescimento do investimento residencial responde às mudanças na inflação de preço dos imóveis. As simulações numéricas mostram que nosso modelo preserva os resultados convencionais do supermultiplicador sraffiano. Como um resultado particular, o aumento na taxa de crescimento do investimento residencial implica uma redução da participação nos imóveis nos ativos reais totais. Baseando-se na bolha imóbiliária recente nos EUA, incluímos dados de inflação do preços dos imóveis (1992-2019) em nossas simulações. Apesar de simples, nossas simulações numéricas são capazes de repoduzir alguns fatos estilizados como o investimento residencial liderando o ciclo econômico bem como a acumulação de capital e um padrão cíclico entre gastos autônomos não criadores de capacidade e grau de utilização da capacidade.

Palavras-Chave: Investimento Residencial; Supermultiplicador sraffiano; Bolha de ativos; Abordagem consistente entre fluxos e estoques, Economia dos EUA. **JEL:** B51, E11, E12, E17, G51, O41, O51

1 Introduction

Non-residential investment is the most scrutinized variable in demand-led growth models so that others expenditures are given a secondary role (BROCHIER; MACEDO E SILVA, 2017). More than a decade after the Great Recession (2008-9), this is still the case for residential investment which continues to receive sparse and unsystematic attention by the literature (CAVERZASI; GODIN, 2014; NIKOLAIDI; STOCKHAMMER, 2017). Despite its absence in theoretical models, there is a growing empirical literature highlighting its macrodynamic relevance (LEAMER, 2007; JORDÀ et al., 2016; FIEBIGER, 2018; FIEBIGER; LAVOIE, 2018).

Sraffian supermultiplier growth model (SSM) establishes an important role to non-capacity creating (NCC) autonomous expenditures such as residential investment. Serrano (1995) and Serrano and Freitas (2017) present a simple version of the SSM model to highlight it as an alternative closure for heterodox growth theory. More recently, departing from neo-Kaleckian framework, Allain (2015) and Lavoie (2014, 2016) have reached similar results to SSM model.

Different NCC autonomous expenditures have been included in this framework. For instance, some scholars have investigated the macroeconomic implications of both debt-financed (PARIBONI, 2015; FAGUNDES; FREITAS, 2018; MANDARINO et al., 2020) and financial wealthfinanced consumption (BROCHIER; MACEDO E SILVA, 2019). The same applies to government expenditures (ALLAIN, 2015; DUTT, 2020) and exports (NAH; LAVOIE, 2017).

Even though these works emphasize the relevance of some NCC autonomous expenditures, residential investment has received little attention. Zezza (2008) and Nikolaidi (2015) include residential investment in a SFC model with others objectives than its implications to economic growth and business cycles. In a recent contribution, Dejuán and McCombie (2018) present an SSM model with residential investment. They build a model in order to analyze the destabilizing effects of household over-indebtedness without exploring the determinants of residential investment.

This paper is a first step in building the connection between house price inflation and residential investment whitin a demand-led growth model. In order to do so, we build a fully specified parsimonious Sraffian supermultiplier stock-flow consistent model (SSM-SFC) with residential investment.

The remainder of this paper is organized as follows. Section 2 discuss some residential investment related stylized facts for the US economy and its macroeconomic implications. Section 3 presents a SSM-SFC model with asset bubbles and two real assets: firms' capital and household' real estate. Section 4 evaluates short- and long-run equilibria as well as traverse in order to assess the consequences of the inclusion of residential investment to the output level, growth rate and to stock-flow ratios. Next, Section 5 evaluates this relations through numerical simulations. Inspired by the U.S. 2000s housing bubble episode, the experiments are: decrease in wage-share (Section 5.1); increase in real estate inflation (Section 5.2); and an increase in interest rate (Section 5.3). In this same Section, we also plug houses own rate of interest observed data for the U.S. (from 1992 to 2019) into our model in order to compare simulations' results with the stylized facts presented previously. Section 6 offers some concluding remarks while Appendix A provides simulation's parameters and baseline values and Appendix B presents a preliminary sensibility analysis.

2 Empirical motivation

A growing body of empirical literature on demand-led growth has evaluated the role of NCC autonomous expenditures. Freitas and Dweck (2013) present a growth accounting decomposition for Brazil from 1970 to 2005 and report the relevance of those expenditures in describing Brazilian GDP growth rate. Braga (2020) shows evidence that economic growth and non-residential investment are explained by NCC autonomous expenditures in the Brazilian economy from 1962 to 2015. For the U.S., Girardi and Pariboni (2016) show that NCC autonomous expenditures have permanent effects on growth rate. Haluska et al. (2020) employ Granger-causality tests to assess the stability of the SSM for the US (1987-2017) and report a causality from NCC autonomous expenditures to the marginal propensity to invest, as expected. Finally, Girardi and Pariboni (2020) bring evidence that those expenditures determine investment share on GDP for twenty OECD countries.

However, there still is a lack of studies on the role of residential investment specifically. It is worth mentioning that the discussion about this NCC autonomous expenditure is largely based on Green (1997) pioneer work. Based on Granger Causality and cointegration tests for the US from 1959-1992, this is one of the first papers to indicates that residential investment leads the business cycle. Subsequently, Leamer (2007) concludes that this pattern occurs at least since the post-war period. More precisely, Leamer (2007, p. 8) describes US business cycles as follows: "[f]irst homes, then cars, and last business equipment". Recently, Fiebiger (2018) and Fiebiger and Lavoie (2018) also report residential investment as an important determinant of business cycles for the US based on causal narratives. Alternatively, Huang et al. (2020) estimate a Structural Vector Autoregressive (SVEC) model in a time-scale framework for the OECD countries to assess both prediction and causality relations stated by Leamer (2007). They report that residential investment predicts the US macroeconomic fluctuation and housing related variables (house prices, real mortgage rate — deflated by a consumer price index — and credit spread) lead the business cycle in all G7 countries.

After the Great Recession (2008-2009), there has been growing macroeconometric stud-

ies on housing. However, most of them have emphasized house prices and not residential investment. Goodhart and Hofmann (2008) for instance, estimate a time-series fixed effects panel data for 17 industrialized countries from 1970 to 2006. They report a multidirectional relation between money, credit, house prices and GDP growth and have found stronger effects during housing booms¹. Wood and Stockhammer (2020) report that house prices are relevant for describing household indebtedness from 1980 to 2017 in 18 advance economies. However, both studies do not include residential investment. Arestis and González-Martínez (2014), on the other side, include residential investment. Using a ARDL model for 17 OECD countries from 1970 to 2013, the authors report that banking credit and real house prices are the most statistically significant variables for real residential investment in the US. Although those approaches are interesting, they fail to take into account the connection between asset bubbles and aggregate demand.

From this review of recent empirical literature, it is noticeable that few macroeconometric studies have investigated residential investment in a systematic way. In this paper, we argue that besides this growing body of literature that recognizes the macroeconomic importance of residential investment, little progress has been made in connecting it to house price bubbles. On the following subsection, we present some residential investment-related stylized facts in order to highlight its relevance for the US business cycle which will be compared to the theoretical model in Section 5.4. Next, we analyze the connection between residential investment, real estate inflation and mortgage interest rate during the U.S. housing bubble episode.

2.1 Residential investment stylized facts

As discussed before, both Green (1997) and Learner (2007) made it clear how important this particular expenditure is to USA business cycle. In this subsection, we show some residential investment stylized facts for the US in more detail.

Figure 1 shows how residential investment dynamics help to predict recessions. Recessions are anticipated by a reduction of residential investment share on GDP, while the expansion of those expenditures precedes economic recovery. The fall of residential investment in 1966-67 are an exception because the increase of military expenditures due to Vietnam War offsets an eventual economic downturn (LEAMER, 2007, p. 20). Another exception is the dot-com bubble 2000 crisis that was not caused by residential investment.

In order to depict the relation between residential investment and business cycle, we present Figure 2 in which each cycle is represented in a different panel². Residential investment-GDP ratio and rate of capacity utilization — as a proxy for business cycle — are presented on vertical and horizontal axis respectively. Economic recovery is generally characterized by residential investment growing faster than GDP. Both residential investment share on GDP and capacity utilization increase as a consequence of higher residential investment growth rate. Accordingly to the Sraffian Supermultiplier model, we can interpret subsequent non-residential investment increase as a result of capital stock adjustment principle. This increase

¹Arestis and González (2014) also found a direct relationship between house prices and credit volume based on cointegration and error correction techniques for 9 OECD countries from 1970 to 2011.

²Similar reasoning can be found in Fiebiger and Lavoie (2018). Unlike them, we plot only residential investment without including other households expenses financed by credit.

Figure 1: Residential Investment as share of GDP



Source: Federal Reserve Bank of St. Louis, authors' elaboration

implies GDP to grow faster than residential investment, therefore reducing both its share on GDP and rate of capacity utilization. As a result of economic burst, rate of capacity utilization falls and the cycle ends. This pattern is more evident in the 1970-75, 1982-91 and in the Great Recession.

2.2 Housing bubble and residential investment

Once we understand the relevance of residential investment to describe the U.S. business cycle, it is important to investigate its determinants. There are at some key variables to assess the residential investment behavior. The first one is the mortgage interest rate, which determines the financial cost of buying houses and the weight of debt-service on house investors' income. The other is the house price inflation. The one who owns a house — or intend to buy one — takes its price variation in consideration for speculative reasons or just to prevent capital loss and reductions of net worth.

Based on SRAFFA's (1932) commodity rate of interest, Teixeira (2015) proposes the socalled houses own rate of interest. Estimated by deflating mortgages interest by houses price inflation, this particular real interest rate is the most relevant for house buyers since it is the real cost in real estate from buying houses (TEIXEIRA, 2015, p. 53). This particular interest rate is shown in Equation 1 in which *own* stands for houses own rate of interst, r_{mo} for mortgage interest rate and π for house price inflation.

$$own = \left(\frac{1+r_{mo}}{1+\pi}\right) - 1\tag{1}$$

During a housing bubble period, it is real estate inflation that governs own's interest rate movements. Therefore, the lower this rate is, the greater the capital gains (in real estate) for speculating with real estate will be. This negative relation between houses own interest rate and residential investment is shown in Figure 3 in which this particular real interest

Figure 2: Share of residential investment and capacity utilization during business cycles (Dots size grow in time)



Source: Federal Reserve Bank of St. Louis, authors' elaboration.

rate has been gradually decreased over the real estate boom (2002-5). Additionally, Figure 3 illustrates this procedure is more adequate than a consumer price index deflation — as Fair (2013, p. 143–6) does — to describe residential investment growth rate³.

In summary, we presented some stylized facts that highlights the relevance of residential investment for the U.S. business cycle and the relevance of house bubbles to the residential investment. In the next section, we build a fully specified parsimonious Sraffian supermultiplier stock-flow consistent model (SSM-SFC) to deal with these stylized facts.

3 A Sraffian supermultiplier SFC model with residential investment

3.1 General equations

Our model is the most parsimonious as possible: a closed capitalist economy without government sector. Output (Y) is determined by a fixed combination of a homogeneous labor (L) input with homogeneous fixed business capital (K_f) . For simplicity, we put technological progress, depreciation and goods inflation aside so investment is presented in net terms

³Based on this concept, Petrini (2020) estimated time series econometric model for the U.S. (1992 to 2019) and presents empirical evidence that residential investment growth rate and houses own rate of interest have a common negative long-run trend. Furthermore, Petrini (2020) also reports a unidirectional long-run causality from houses own rate of interest to residential investment growth rate.

Figure 3: Residential investment growth rate vs. Houses Own rate of interest



Source: U.S. Bureau of Economic Analysis, Authors' elaboration

and all variables — except for houses — are measured in real terms. Assuming a Leontief production function (Equation 2) and that growth is not constrained by labor scarcity, full capacity output (Y_{FC}) is determined by firms' capital stock (Equation 3):

$$Y_{FC} = \min(Y_L, Y_K) \tag{2}$$

$$Y_{FC} = \frac{K_{f-1}}{v} \tag{3}$$

$$u = \frac{Y}{Y_{FC}} \tag{4}$$

where Y_L and Y_K stands for full employment and full capacity output respectively, v is exogenous capital-output ratio and u is rate of capacity utilization.

We further assume a social structure composed by both workers (denoted by subscript w) and capitalists (denoted by subscript k) households. Thus, demand determined output level (Y, Equation 7) is the sum of workers and capitalists consumption (C_w and C_k respectively) and both households and firms investment (I_h and I_f respectively) and only the latter creates capacity to the business sector of the economy:

$$C = C_w + C_k \tag{5}$$

$$I_t = I_f + I_h \tag{6}$$

$$Y = \overbrace{[C_w + \underbrace{C_k + I_h}]}^{\text{Households}} + \overbrace{[I_f]}^{\text{Firms}}$$
(7)

In other words, from a institutional sectors perspective, household expenditures have two components (consumption and residential investment) and firms just one (non-residential investment). So, the novelty of this model is the inclusion of a second investment component all made by household sector and held by capitalists households for simplicity. Therefore, this economy produces two types of real assets: firms productive capital (K_f) and households houses (K_h) :

$$K = K_f + K_h \tag{8}$$

Denoting the houses share in total real assets as k (Equation 9), we can rewrite equation 8 as:

$$k = \frac{K_h}{K}$$

$$K = (1 - k) \cdot K + k \cdot K$$
(9)

Following Sraffian literature, functional income distribution is determined by historicalinstitutional factors and class struggle. As consequence, wage-share (ω) is considered exogenous to our model and define total wages as (W, Eq. 10):

$$W = \omega \cdot Y \tag{10}$$

Table 1 presents the balance sheet matrix for all institutional sectors. Capitalists households hold financial wealth as bank deposits (M) and residential investment is financed by mortgages (MO). Capitalists' total net wealth (NW_k) is the sum of their net financial wealth (V_k) and real assets (*i.e.* houses, K_h). Table 2 presents both transactions flows and the flow of funds matrix. This table shows all economic relations between institutional sectors ensuring that there is no "black holes" so all financial and real transaction are explicitly defined (GODLEY; LAVOIE, 2007; MACEDO E SILVA; DOS SANTOS, 2011).

In this model, capitalist consumption (C_k) is fully autonomous and financed by loans (L_k) while workers consumption (C_w) is fully induced by their wages. We assume that workers expend what they earn while capitalists earn what they expend, so workers financial and real wealth are both null. Firms finance their investment primarily by undistributed profits (FU) and the residual by bank loans (L_f) — thus they do not hold deposits. Banks create credit *ex nihilo* and then collect the deposits, paying the same interest rate that they charge. On the following subsections, we will present the equations of each of those institutional sectors.

 Table 1: Balance Sheet matrix

| | Workers | Capitalists | Firms | Banks | \sum |
|-----------------------------|---------|-------------|--------|--------|--------|
| Deposits | | +M | | -M | 0 |
| Loans | | $-L_k$ | $-L_f$ | +L | 0 |
| Mortages | | -MO | | +MO | 0 |
| \sum Net Financial Wealth | | V_k | V_f | V_b | 0 |
| Capital | | | $+K_f$ | | $+K_f$ |
| Houses | | $+K_{hd}$ | | | $+K_h$ |
| \sum Net Wealth | | NW_k | NW_f | NW_b | +K |

Source: Authors' Elaboration

| | Workers | Capitalists | | Firms | | Banks | Total |
|----------------------------|---------|-------------------------|--------------|----------------------|----------|-------------------------|--------|
| | | Current | Capital | Current | Capital | - | \sum |
| Consumption | -Cw | $-C_k$ | | +C | | | 0 |
| Non-residential Investment | | | | $+I_f$ | $-I_f$ | | 0 |
| Residential Investment | | | $-I_h$ | $+I_h$ | | | 0 |
| [Output] | | | | [Y] | | | [Y] |
| Wages | +W | | | -W | | | 0 |
| Profits | | +FD | | -FT | +FU | | 0 |
| Deposits interest rate | | $+r_m \cdot M_{-1}$ | | | | $-r_m \cdot M_{-1}$ | 0 |
| Loans interest rate | | $-r_l \cdot L_{k-1}$ | | $-r_l \cdot L_{f-1}$ | | $+r_l \cdot L_{-1}$ | 0 |
| Mortages interest rates | | $-r_{mo} \cdot MO_{-1}$ | | | | $+r_{mo} \cdot MO_{-1}$ | 0 |
| Subtotal | | $+S_h$ | $-I_h$ | | $+NFW_f$ | $+NFW_b$ | 0 |
| Change in deposits | | $-\Delta M$ | | | | $+\Delta M$ | 0 |
| Change in mortgages | | | $+\Delta MO$ | | | $-\Delta MO$ | 0 |
| Change in loans | | $+\Delta L_k$ | | $+\Delta L_f$ | | $-\Delta L$ | 0 |
| Total | | 0 | 0 | 0 | 0 | 0 | 0 |

Table 2: Transactions flow matrix and flow of funds

Source: Authors' Elaboration

3.2 Firms

In order to produce, firms purchase capital goods $(-I_f \text{ in capital account})$ and hire workers, whom total remuneration is the economy wage bill. Firms total profits (FT, Equation 11) are a residual between sales (Y) and total wages (W). Firms retain part (γ_F) of profits net of interest payments (FU, Equation 12) — to reinvest — and distribute the remainder to capitalists (FD, Equation 13):

$$FT = Y - W = FD + FU \tag{11}$$

$$FU = \gamma_F \cdot (FT - r_l \cdot L_{f-1}) \tag{12}$$

$$FD = (1 - \gamma_F) \cdot (FT - r_l \cdot L_{f-1}) \tag{13}$$

Firms (non-residential) investment is fully induced by the level of effective demand (Eq. 14), and its growth rate changes accordingly to the capital stock adjustment principle (FRE-ITAS; SERRANO, 2015). Equation 15 is a simple way to describe this mechanism. According to it, the marginal propensity to invest (h) endogenously adjust to discrepancies between actual and normal utilization rates (u and u_N , respectively). For this mechanism to take place, the adjustment parameter (γ_u) must be sufficiently small and non-negative⁴. As a consequence, productive capacity gradually adjusts to effective demand.

$$I_f = h_{t-1} \cdot Y \tag{14}$$

 $^{^{4}}$ The size of this parameter guards a fundamental relation to the stability of the model, as shown by Freitas and Serrano (2015).

$$\Delta h = h_{t-1} \cdot \gamma_u \cdot (u - u_N) \tag{15}$$

$$\Delta K_f = I_f \tag{16}$$

Firms finance investment that exceeds undistributed profits by bank loans, paying an interest rate on it (r_l) charged by the banks. We assume an elastic supply of credit for investment. Moreover, tables 1 and 2 show firms net wealth (NW_f) and net financial balance (NFW_f) explicitly:

$$\Delta L_f = I_f - FU \tag{17}$$

$$NFW_f = FU - I_f \tag{18}$$

$$NW_f = K_f - L_f \tag{19}$$

$$r_g = \frac{(1-\omega) \cdot u}{v} \tag{20}$$

$$r_n = r_g - r_l \cdot \frac{L_{f-1}}{K_f} \tag{21}$$

where r_g and r_n denotes gross and net profit rate respectively.

3.3 Banks

As in most part of SFC literature, banks do not have an active role in this model. They create money as credit is demanded and just after they collect deposits (LE BOURVA, 1992). Firms finance part of their investment with credit (L_f) and capitalists households finance all their residential investment by mortgages (MO) and consumption by loans (L_k) , as already mentioned. For simplicity, we assume null bank spreads $(\sigma_{mo} = \sigma_l = 0)$ so interest rate on mortgages (r_{mo}) and on loans (r_l) are the same as on deposits (r_m) which is exogenously determined by banks. Banks net balances (NFW_b) are defined by interests received net of interests payments. As those interests are the same, banks net wealth is necessarily zero (see table 1) and deposits are residuum:

$$L = L_f + L_k \tag{22}$$

$$r_l = (1 + \sigma_l) \cdot r_m \tag{23}$$

$$r_{mo} = (1 + \sigma_{mo}) \cdot r_m \tag{24}$$

$$r_m = \overline{r}_m \tag{25}$$

$$NFW_b = r_{mo} \cdot MO_{-1} + r_l \cdot L_{-1} - r_m \cdot M_{-1}$$

$$NFW_b = \Delta MO + \Delta L - \Delta M$$
(26)

$$NW_b = V_b \equiv 0 \tag{27}$$

$$\Delta M = \Delta L + \Delta M O \tag{28}$$

3.4 Households

3.4.1 Workers

As mentioned before, we assume that workers expend (C_w) what they earn (W). For simplicity, we consider that wages are the only source of workers' disposable income (YD_w) and do not have access to consumption loans, so worker' saving (S_{hw}) are null. Therefore, accordingly to our hypothesis, workers do not hold both net financial (NFW_w) nor total wealth (V_w) .

 $S_w = 0$

$$C_w = W \tag{29}$$

$$YD_w = W \tag{30}$$

$$S_w = YD_w - C_w \tag{31}$$

$$NFW_w = S_w = 0 \tag{32}$$

$$V_w = 0 \tag{33}$$

3.4.2 Capitalists

This is the most complex institutional sector of our model. We assume consumption (C_k) is fully-autonomous and financed by loans (L_k) . Disposable income (YD_k) is the sum of distributed profits and received interests on deposits, net of interests payments on both mortgages and loans. Capitalists savings (S_k) are disposable income net of consumption. At odds with SFC literature, savings are not equal to net balance $(NFW_k, Equation 37)$ since we have included residential investment.

$$\Delta L_k = C_k \tag{34}$$

$$YD_k = FD + \bar{r}_m \cdot M_{-1} - r_{mo} \cdot MO_{-1} - r_l \cdot L_{k_{-1}}$$
(35)

$$S_k = YD_k - C_k \tag{36}$$

$$NFW_k = S_k - I_h \tag{37}$$

As mentioned before, capitalist households are the only institutional sector investing in houses which are financed by mortgages as in equation 38. Thus, capitalists' total debt stock (D) is the sum of mortgage and consumption loans (Equation 39)

$$\Delta MO = I_h \tag{38}$$

$$D = MO + L_k \tag{39}$$

Next, we present residential investment growth rate (g_{I_h}) as determined by houses own rate of interest (*own*, equation 1) as introduced by Teixeira (2015) and discussed in section 2.

$$I_h = (1 + g_{I_h}) \cdot I_{h_{-1}} \tag{40}$$

$$g_{I_h} = \phi_0 - \phi_1 \cdot own \tag{41}$$

where ϕ_0 represents long-term determinants of residential investment (*e.g.* demographic factors, housing and credit policies, etc.)⁵ while ϕ_1 captures houses own rate of interest as described in Section 2.2.

Accordingly to our hypothesis, nominal (V_{nk}) and real net wealth (V_k) are distinguished only by the inclusion of house price (p_h) and are defined as follows:

$$V_k = K_{hd} + M - L_k - MO \tag{42}$$

$$V_{nk} = K_{hd} \cdot p_h + M - L_k - MO \tag{43}$$

In order to fulfill our goals, we employ FREITAS; CHRISTIANES'S (2020) procedure in which NCC autonomous expenditure (Z) composition (R) remains unchanged.

$$Z = C_k + I_h \tag{44}$$
$$\frac{C_k}{Z} + \frac{I_h}{Z} = R + (1 - R)$$

which allows us to rewrite both residential investment and capitalists consumption in terms of residential investment (Eq. 46):

$$C_k = R \cdot Z \tag{45}$$

$$Z = \frac{I_h}{(1-R)} \tag{46}$$

⁵For an early discussion about long-term determinants of residential investment see Grebler et al. (1956). For a historical-institutional discussing of mortgage markets, see Green and Wachter (2005).

$$C_k = I_h \cdot \frac{R}{(1-R)} \tag{47}$$

Finally, we can describe NCC autonomous expenditure growth rate as follows:

$$g_{\mathrm{C}_{\mathrm{k}}} = g_{\mathrm{Z}} = g_{\mathrm{I}_{\mathrm{h}}} = \phi_0 - \phi_1 \cdot own \tag{48}$$

In this section, we presented a fully-specified parsimonious model to connect house bubbles with aggregate demand. In the next Section, we analyze the dynamics from short- to long-run equilibria.

4 From short- to long-run equilibria

In this Section, we show the implications of residential investment inclusion into a SSM-SFC model. First, we present the short-run dynamics and then move to the traverse and then to the long-run equilibrium (denoted by \star).

4.1 Short-run good market equilibrium

In this model, real output (equation 7) is the sum of household consumption (equation 5) and both types of investment (equation 6). If we replace equations 10 and 14 into 7 and considering equation 44 we get the short-run GDP level which is determined both by NCC expenditures (Z_t) and the supermultiplier (inverse of Equation 49 denominator)

$$Y_t = \frac{Z_t}{1 - h_t - \omega} \tag{49}$$

and replacing Equation 46 in the previous one

$$Y_t = \frac{I_h}{(1-R)(1-h_t - \omega)}$$
(50)

since R is non-negative and lower than one, the Keynesian stability condition is $h_t + \omega < 1$.

Next, dividing equation 50 by 3, replacing residential investment growth rate by Equation 41 and rearranging, we get the short-run equilibrium utilization rate (Equation 51). In this model, residential investment growth rate determines GDP growth rate. When the latter accelerates, rate of capacity utilization increases as shown by Equation 51:

$$u_t = \frac{v}{(1-R)(1-h_t-\omega)} \frac{I_{h_{t-1}}}{K_{f_{t-2}}} \frac{(1+g_{I_h})}{(1+g_{K_{t-1}})}$$
(51)

Replacing equation 41 in Equation 51 we make explicit the functional form of residential investment growth rate as one of the determinants of rate of capacity utilization as shown in Equation 52:

$$u_t = \frac{v}{(1-R)(1-h_t-\omega)} \frac{I_{h_{t-1}}}{K_{f_{t-2}}} \frac{(1+\phi_0-\phi_1\cdot own_t)}{(1+g_{K_{t-1}})}$$
(52)

Next, we revisit Equation 51 in order to present houses share on total capital stock (k). To do so, we express firms' capital in terms of houses. Then, dividing both sides of equation 51 by houses and after some algebraic manipulations, we get houses-to-capital ratio (Equation 53)

$$k = \frac{(1-R) \cdot (1-h_t - \omega)}{h_t + (1-R) \cdot (1-h_t - \omega)}$$
(53)

4.2 Traverse and long-run equilibrium

In this subsection, we present traverse and long-run equilibrium equations. According to equation 51, when aggregate demand and capacity output grow at different rates, capacity utilization will change. The discrepancy between actual and normal rate of capacity utilization triggers marginal propensity to invest adjustment mechanism (see Equation 15). During the adjustment process, both supermultiplier and NCC autonomous expenditure share on GDP changes. Equation 54 presents aggregate demand during the traverse:

$$g_t = g_Z + \frac{\Delta h}{1 - \omega - h_t} \tag{54}$$

This process continues as long as GDP growth rate moves towards NCC autonomous expenditure growth rate (in this case, residential investment and capitalist consumption).

As mentioned before, firms' marginal propensity to invest reacts to discrepancies between the rate of capacity utilization and the normal one. This adjustment process continues until actual and normal rate of capacity utilization are equal:

$$u \to u^* = u_N \Leftrightarrow g \to g^* = g_Z = g_{I_h}$$

and long-run marginal propensity to invest will be:

$$h^{\star} = g^{\star} \cdot \frac{v}{u^{\star}} \tag{55}$$

Finally, replacing Equation 55 into Equation 49 we obtain long-run GDP level as shown in Equation 56

$$Y^{\star} = \frac{Z}{\left(1 - \omega - g^{\star} \cdot \frac{v}{u^{\star}}\right)} \tag{56}$$

Once again, we can show the long-run position making the residential investment growth rate explicit as in Equation 57

$$Y^{\star} = \frac{I_h}{(1-R)\left(1-\omega - g_{I_h}^{\star} \cdot \frac{v}{u^{\star}}\right)}$$
(57)

Next, we move towards the analysis of the particularities of our model. To do so, we replace Equation 55 in 53, we obtain long-run ratio between houses and total capital stock (denoted by k^*):

$$k^{\star} = 1 - \frac{h^{\star}}{h^{\star} + (1 - R)(1 - h^{\star} - \omega)}$$
(58)

Before moving to the numerical simulations, we present some steady growth stock ratios in order to shed some lights in the dynamic process of the model. At odds with literature, we do not normalize the stocks by the total capital stock, but by the economically relevant capital (firms' capital stock or houses) type. Thus, dividing Equation 17 by firms' capital stock and making some algebraic manipulation, we obtain steady growth loans' ratio to firms' capital stock (ℓ^* , Equation 59):

$$\Delta\left(\frac{L_f}{K_f}\right) = \frac{I_f - FU}{K_f} - \ell_f^* \cdot g^* = 0$$

$$\ell_f^* = 1 - \gamma_F\left(\frac{r_g^* - r_m}{g^* - \gamma_F \cdot r_m}\right)$$
(59)

Thus, replacing equation 59 into 21 to obtain net profit rate in the long-run (see Equation 60)

$$r_n^{\star} = r_g^{\star} - r_m \cdot \left(1 - \gamma_F \left(\frac{r_g^{\star} - r_m}{g^{\star} - \gamma_F \cdot r_m} \right) \right) \tag{60}$$

Next, we rewrite capitalists autonomous expenditure in terms of residential investment (see Equation 47). Then, we present capitalists' loans to houses stock ratio (Equation 61):

$$\Delta\left(\frac{L_k}{K_{HD}}\right) = \frac{C_k}{K_{HD}} - \ell_k^\star \cdot g^\star = 0$$
$$\ell^\star = \frac{R}{1-R} \tag{61}$$

The same procedure is also applied to find mortgage to house stock ratio (mo^* , Equation 62):

$$\Delta \left(\frac{MO}{K_{HD}}\right) = \frac{\Delta MO}{K_{HD}} - mo^* \cdot g^* = 0$$
$$mo^* = 1 \tag{62}$$

Thus, adding Equations 61 and 62 and, we get households capitalists' total debt in terms of houses $(d^*, \text{ Equation 63})$

$$d^{\star} = 1 + \frac{R}{1 - R}$$

$$d^{\star} = \frac{1}{1 - R}$$
(63)

Finaly, we can express deposits share on total capital stock $(m^*, \text{ Equation 64})$ in terms of previous stock ratios:

$$\frac{M}{K} = \frac{MO + L_k + L_f}{K}$$
$$\frac{M}{K} = \frac{MO}{K_{HD}} \cdot \frac{K_{HD}}{K} + \frac{L_k}{K_{HD}} \cdot \frac{K_{HD}}{K} + \frac{L_f}{K_f} \cdot \frac{K_f}{K}$$
$$m^* = mo^* \cdot k^* + \ell^*_k \cdot k^* + \ell^*_f \cdot (1 - k^*)$$
(64)

5 Numerical simulations

In this Section, we present the results of the following numerical experiments: (i) wageshare decrease; (ii) house price inflation; (iii) benchmark interest rate increase. In order to evaluate if our model is able to reproduce some stylized facts, we also perform a numerical simulation with US data of houses own rate of interest (from 1992 to 2019). Before we move foward, it is worth mentioning that we use FAZZARI et al.'s (2020) parameter values calibrated for the U.S. economy for a similar time range (from 1980 to 2016). Our first experiment assess if income distribution has a level effect on output — as in (MANDARINO et al., 2020) — or growth rate effect — as in (BROCHIER; MACEDO E SILVA, 2019). Real estate inflation increase experiment is motivated by recent US experience (from 1992 to 2019) as discussed in Section 2 while the last simulation aims to evaluate indebtedness stability. Table 4 in Appendix A presents the parameters of simulation and Table 3 compare each result to baseline.

5.1 Wage-share decrease

A wage-share decrease has permanent negative impact on output level — due to changes in the supermultiplier — and temporary negative effects on degree of capacity utilization (see Figure 4 A). So, aggregate demand growth level is temporarily smaller than baseline as a result of the lower supermultiplier. As a consequence of this negative level effect, both accumulation growth rate and marginal propensity to invest temporally decline while NCC autonomous expenditures share on GDP increases. Since NCC autonomous expenditures growth rate remains unchanged and its share on GDP increases, aggregate demand grows faster than accumulation rate. As a result, degree of capacity utilization is higher than the normal one. During the traverse, marginal propensity to invest endogenously adjust to discrepancies between actual and normal capacity utilization rates. Consequently, nonresidential investment growth rate increases faster than aggregate demand. This endogenous adjustment process continues as long as actual rate of capacity utilization is different from the normal one. In summary, we report standards SSM model results: (i) marginal propensity to invest decrease is temporally and returns to baseline level; (ii) rate of capacity utilization moves towards normal one; (iii) supermultiplier decreases and autonomous expenditures share of GDP increases; (iv) since autonomous expenditures growth rate does not change, distribution effects on growth rates are temporary.

Despite temporary growth rate effects, wage-share decrease has a permanent effect on house share on total capital stock (see Equation 58 and Figure 5 B). As a consequence of the initially lower accumulation rate, total capital stock also grows at a temporarily lower rate. However, since residential investment growth rate remains unchanged, its share on total capital stock increases.

Finally, we also report a persistent effect on firms' balance sheet due to wage-share decrease. The negative level effect on GDP implies an already mentioned temporally decrease in marginal propensity to invest. As a consequence of the initially lower accumulation rate and higher profit share, firms' loan-to-capital ratio decrease. Thus, according to Equation 60, gross and net profit rate remain persistently close to each other (see Figure 5 D). Therefore, as profits distribution policy remains the same, firms require less external funding so its indebtedness decreases.

5.2 Real estate inflation increase

An increase of real estate inflation implies a higher residential investment growth due to houses own rate of interest decrease. As a result, both GDP growth rate and degree of capacity utilization increase as well. Since firms react to discrepancies between actual and normal degree of capacity utilization rate, non-residential investment growth rate is temporally higher than GDP growth rate due to marginal propensity to invest adjustment. Furthermore, capitalists' disposable income also increases as a result of the already mentioned higher GDP growth rate. Since loans interest remains unchanged, capitalists' indebtedness ratio decreases. During the traverse, gross and net profit rate are temporally close to each other as a result of profits level increase, so firms' indebtedness decreases as well. Therefore, similar to Mandarino et al. (2020), we also report paradox of debt.

In summary, we report SSM standard long-run results: (i) GDP growth rate converges to NCC autonomous expenditure growth rate; (ii) marginal propensity to invest remains persistently higher compared to baseline and; (iii) utilization rate moves gradually towards the normal one.

The most distinct result is real houses share decreases on total capital stock as a result of residential investment growth rate increase. Although counterintuitive, this result is similar to the conventional paradox of debt. This is the case since houses are always equivalent to mortgage debt. Additionally, this result is in line with SSM literature. Firms investment follows capital stock adjustment principle, so a higher firms investment growth rate implies that GDP grows faster than residential investment. Thus, both residential investment share on GDP and degree of capacity utilization decrease. In other words, both autonomous expenditures share on GDP and houses share on real assets decline as a result of the already described non-residential investment positive reaction.

5.3 Interest rate increase

A increase in benchmark interest rate has a persistent effect on long-run growth rate since houses own interest rate increases as well⁶. Non-residential investment growth rate decreases as a result of residential investment growth rate permanent decline, so houses share on real assets increases. Compared to the previous experiments, this shock has opposite effects on long-run growth rates, NCC autonomous expenditure share on GDP, utilization rate and marginal propensity to invest than the previous one (see Figure 4).

In particular, we report a stronger negative effect over both capitalists' and firms' balance sheet than wage-share decrease (see figures 4 and 5). This effect is a result of the temporarily stronger decline of GDP growth rate compared to NCC autonomous expenditure growth rate. As a consequence of lower GDP growth rate, total profits also decreases. Thus, capitalists' disposable income decreases more than debt-financed consumption growth rate. Interest rate increase alone is enough to capitalists' indebtedness level to increase, however it is followed by GDP growth rate decrease, so the overall effect is stronger than wage-share decrease experiment (Section 5.1). Regarding firms' balance sheet, we report a temporarily negative level effect on gross profit rate and a permanent one on net profit rate. So, there is a

⁶Since we assume null spread on both mortgage and loans interest rate, an increase on deposits interest rate also increases the other ones. As a consequence, banks' net financial wealth remains unchanged.

permanent increase in the gap between them due to increase in external funding and to the negative level effect on profits. Therefore, we find a stable debt dynamics for both capitalists and firms (other parameters remaining unchanged).

| | traverse $(h \neq h^{\star})$ | | | Long-run $(h = h^*)$ | | | |
|----------------------------|-------------------------------|----------------|---------------|----------------------|----------------|---------------|--|
| | $\Downarrow \omega$ | $\uparrow \pi$ | $\Uparrow rm$ | $\Downarrow \omega$ | $\uparrow \pi$ | $\Uparrow rm$ | |
| g | - | + | - | 0 | + | - | |
| g_Z | 0 | + | - | 0 | + | - | |
| u | - | + | - | 0 | 0 | 0 | |
| h | - | + | - | 0 | + | - | |
| k | + | - | + | + | - | + | |
| $\frac{Z}{Y}$ | + | - | + | + | - | + | |
| $r_m \frac{(D-M)}{K_{HD}}$ | + | - | + | 0 | - | + | |

Table 3: Shocks summary (compared to baseline)

Source: Authors' Elaboration



Figure 4: Experiments simulations (I)

Source: Authors' elaboration

5.4 Plugging real data

Finally, we include houses own rate of interest data discussed in section 2 (see Figure 3) into our model. In order to do so, each year corresponds to ten simulated periods for visualization reasons. Additionally, we have abandoned the assumption of a fixed share (R) between residential investment and capitalist consumption. In order to include capitalists



Figure 5: Experiments simulations (II)

Source: Authors' elaboration

consumption without running into asymptotic paths, we defined its growth rate as the geometric average of residential investment growth rate from 1992 to 2019.

Although rudimentary, this procedure allows us to replicate some stylized facts presented in section 2 and in the literature (see Figure 6). Similarly to Figure 2, we report a clockwise relationship between autonomous expenditure share on GDP and rate of capacity utilization. With due mediation, we also report a smooth gravitation of capacity utilization ratio towards the normal one. As expected, NCC autonomous expenditures (notably residential investment) describes accumulation and GDP growth rate. Together these results provide a first step towards the connection between house bubbles and aggregate demand within the Sraffian Supermultiplier framework.

6 Concluding remarks

This paper contributes to demand-led growth agenda, taking in consideration recent efforts of embedding it in a SFC framework. Our novelty is the introduction of residential investment determined by houses own rate of interest in a SSM-SFC model. Residential investment has been included due to recent empirical works showing its relevance for macroeconomic dynamics. Houses' own rate of interest allowed us to connect house bubbles with aggregate demand in a rather parsimonious way.

Our model reports standard results of Sraffian Supermultiplier: (i) utilization rate converges to the normal one through changes on firms' marginal propensity to invest; (ii) GDP growth rate converges to NCC autonomous expenditure growth rate and; (iii) income distribution affects growth rate only during the traverse. A particular feature of our model is the dual composition of capital stock: firms' capacity creating and real estate. The most





Source: Authors' elaboration

distinct result is the decrease of houses share on capital stock due to the increase of residential investment growth rate. Although counterintuitive, this occurs because firms react to the discrepancies between actual and desired utilization rates. In other words, for capacity utilization converges to the normal one, firms' investment needs to grow temporarily faster than residential investment, changing the ratio between houses and total capital stock in the long-run.

Future research should increase the complexity of this model in order to understand other consequences of residential investment. Some extensions could explore other determinants of its growth rate and its effects on banks' net financial wealth. This emerging "housing agenda" should also moves towards institutional grounds. For example, future research could assess which institutional arrangements allow/inhibit the connection between house bubble, credit granting/rationing and financial instability. Nevertheless, this is a little step in a wider research agenda on the role of residential investment for economic growth and business cycles.

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Disclosure statement

No potential conflict of interest was reported by the authors.

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A Numerical appendix

| | Base scenario | $\Delta \phi_0$ | $\Delta \omega$ | Δrm | π |
|---------------|---------------|-----------------|-----------------|-------------|--------|
| α | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| γ_F | 0.0800 | 0.0800 | 0.0800 | 0.0800 | 0.0800 |
| γ_u | 0.0900 | 0.0900 | 0.0900 | 0.0900 | 0.0900 |
| ω | 0.2500 | 0.2500 | 0.2400 | 0.2500 | 0.2500 |
| rm | 0.0100 | 0.0100 | 0.0100 | 0.0120 | 0.0100 |
| σ_l | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| σ_{mo} | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| u_N | 0.8000 | 0.8000 | 0.8000 | 0.8000 | 0.8000 |
| v | 1.2000 | 1.2000 | 1.2000 | 1.2000 | 1.2000 |
| ϕ_0 | 0.0250 | 0.0300 | 0.0250 | 0.0250 | 0.0250 |
| ϕ_1 | 0.1000 | 0.1000 | 0.1000 | 0.1000 | 0.1000 |
| R | 0.7000 | 0.7000 | 0.7000 | 0.7000 | 0.7000 |
| π | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0500 |

Table 4: Parameters of variables

Source: Authors' elaboration

B Sensibility analysis

| Table 5: | Effect of individual parameters |
|----------|---------------------------------|
| | on model stability |

| Parameter | Description | Instability inducing value | Effect of increase |
|------------|--------------------------------|----------------------------|--------------------|
| | | | |
| γ_u | Adjustment speed | 0.65 | Destabilizing |
| ω | wage-share | - | Stabilizing |
| γ_F | Profit distribution policy | - | Destabilizing |
| rm | Deposits interest rate | - | Stabilizing |
| ϕ_0 | g_{I_h} autonomous component | 0.32 | Destabilizing |
| ϕ_1 | own interest rate parameter | - | Destabilizing |
| π | real estate inflation | - | Destabilizing |
| R | C_k share on Z | 0.91 | Stabilizing |

Source: Authors' elaboration